

Q:-  $\int \frac{1}{x^3} + \frac{1}{x^2} dx$

$$= \int x^{-3} dx + \int x^{-2} dx$$

$$= \int \frac{x^{-3+1}}{-3+1} dx + \int \frac{x^{-2+1}}{-2+1} dx$$

$$= \frac{x^{-2}}{-2} + \frac{x^{-1}}{-1} + C$$

$$= -\frac{1}{2x^2} - \frac{1}{x} + C$$

Q:-  $\int \left( 6e^x - \frac{3}{x^2} \right) dx$

$= \int 6e^x dx - \int 3x^{-2} dx$

$= \int 6e^x dx - 3 \int \frac{x^{-2+1}}{-2+1} dx$

Notes

$= 6e^x - 3 \cdot \frac{x^{-1}}{-1} + C$

$= 6e^x + \frac{3}{x} + C$  *Ans*

$$\text{Q:-} \int x^{\frac{3}{4}} \left( 2x^{\frac{2}{3}} + 6x^{\frac{1}{2}} \right) dx$$

$$= \int \left( 2x^{\frac{17}{12}} + 6x^{\frac{5}{4}} \right) dx$$

$$= 2 \int \frac{x^{\frac{17}{12} + 1}}{\frac{17}{12} + 1} dx + 6 \int \frac{x^{\frac{5}{4} + 1}}{\frac{5}{4} + 1} dx$$

$$= 2 \int \frac{x^{\frac{17+12}{12}}}{\frac{17+12}{12}} dx + 6 \int \frac{x^{\frac{5+4}{4}}}{\frac{5+4}{4}} dx$$

$$= 2 \cdot \frac{x^{\frac{29}{12}}}{\frac{29}{12}} + 6 \cdot \frac{x^{\frac{9}{4}}}{\frac{9}{4}} + C$$

$$= \frac{2 \cdot 12}{29} x^{\frac{29}{12}} + \frac{6 \cdot 4}{9} x^{\frac{9}{4}} + C$$

$$= \frac{24}{29} x^{\frac{29}{12}} + \frac{8}{3} x^{\frac{9}{4}} + C$$

$$\text{Q:- } \int \sqrt{x} \left( x^{\frac{2}{3}} + 2x^{\frac{1}{2}} + 5x \right) dx$$

$$= \int x^{\frac{1}{2}} \left( x^{\frac{2}{3}} + 2x^{\frac{1}{2}} + 5x \right) dx$$

$$= \int \left( x^{\frac{7}{6}} + 2x + 5x^{\frac{3}{2}} \right) dx$$

$$= \int \frac{x^{\frac{7}{6}+1}}{\frac{7}{6}+1} dx + 2 \int \frac{dx^{1+1}}{1+1} dx + 5 \int \frac{x^{\frac{3}{2}+1}}{\frac{3}{2}+1} dx$$

$$= \int \frac{x^{\frac{13}{6}}}{\frac{13}{6}} dx + 2 \int \frac{x^2}{2} dx + 5 \int \frac{x^{\frac{5}{2}}}{\frac{5}{2}} dx + C$$

$$= \frac{6}{13} x^{\frac{13}{6}} + \frac{2 \cdot x^2}{2} + \frac{5 \times 2}{5} x^{\frac{5}{2}} + C$$

$$= \frac{6}{13} x^{\frac{13}{6}} + x^2 + 2x^{\frac{5}{2}} + C$$

THURSDAY

$$Q. \int (4x+2)(3+4x) dx$$

$$= \int (12x + 16x^2 + 6 + 8x) dx$$

$$= \int 16x^2 + 20x + 6 dx$$

$$= 16 \int x^2 dx + 20 \int x dx + 6 \int dx$$

$$= 16 \int \frac{x^{2+1}}{2+1} dx + 20 \int \frac{x^{1+1}}{1+1} dx + 6x + C$$

$$= \frac{16}{3} x^3 + \frac{10}{2} x^2 + 6x + C$$

$$= \frac{16}{3} x^3 + 10x^2 + 6x + C$$